

1) Compute the probability of X successes.

$$n = 7, X = 6, p = 0.3 \quad q = 1 - p = 0.7$$

- A) 0.857 B) 0.996 C) 0.3 D) 0.004

1) D

$P(x=6) = {}^7C_6 (0.3)^6 (0.7)^1 = 0.00357\dots$ On Calculators use Binom pdf on TI84 or Bpd on Casio

2) Determine the indicated probability for a binomial experiment with the given number of trials n and the given success probability p .

$$n = 13, p = 0.7, P(\text{Fewer than 4})$$

- A) 0.0040 B) 0.0007 C) 0.0001 D) 0.9993

2) B

$$P(\text{fewer than 4}) = P(0) + P(1) + P(2) + P(3) = 0.0000001594 + 0.0000048361 + 0.000067706 + 0.00057926 = 0.00065196\dots \Rightarrow 0.0007$$

$$P(0) = {}^{13}C_0 (0.7)^0 (0.3)^{13} = 0.0000001594\dots$$

$$P(1) = {}^{13}C_1 (0.7)^1 (0.3)^{12} = 0.0000048361\dots$$

$$P(2) = {}^{13}C_2 (0.7)^2 (0.3)^{11} = 0.000067706\dots$$

$$P(3) = {}^{13}C_3 (0.7)^3 (0.3)^{10} = 0.00057926\dots$$

3) Determine the indicated probability for a binomial experiment with the given number of trials n and the given success probability p .

$$n = 11, p = 0.5, P(9 \text{ or more})$$

- A) 0.9673 B) 0.0327 C) 0.1133 D) 0.0059

3) B

$$P(9 \text{ or more}) = P(9) + P(10) + P(11) = 0.026855 + 0.0053711 + 0.00048828 = 0.032715\dots$$

$$P(9) = {}^{11}C_9 (0.5)^9 (0.5)^2 = 0.026855$$

$$P(10) = {}^{11}C_{10} (0.5)^{10} (0.5)^1 = 0.0053711$$

$$P(11) = {}^{11}C_{11} (0.5)^{11} (0.5)^0 = 0.00048828$$

On Casio, Find Bcd ($x=8$): $1 - 0.967285 = 0.032715$; on a TI84 binomcdf

4) Determine the indicated probability for a binomial experiment with the given number of trials n and the given success probability p .

$$n = 14, p = 0.1, P(3 \text{ or fewer})$$

- A) 0.8416 B) 0.9559 C) 0.0441 D) 0.9908

4) B

$$P(3 \text{ or fewer}) = P(0) + P(1) + P(2) + P(3) = 0.22876 + 0.35586 + 0.25701 + 0.11423 = 0.95586$$

$$P(0) = {}^{14}C_0 (0.1)^0 (0.9)^{14} = 0.22876$$

$$P(1) = {}^{14}C_1 (0.1)^1 (0.9)^{13} = 0.35586$$

$$P(2) = {}^{14}C_2 (0.1)^2 (0.9)^{12} = 0.25701$$

$$P(3) = {}^{14}C_3 (0.1)^3 (0.9)^{11} = 0.11423$$

Or, on a graphing calculator, Bcd or binom cdf for $x=3$

5) In a large bag of marbles, 30% of them are red. A child chooses 4 marbles from this bag. If the child chooses the marbles at random, what is the chance that the child gets exactly three red marbles?

- A) 0.176 B) 0.076 C) 0.265 D) 0.108

5) B

$$p = 0.30 \quad x = 3 \quad n = 4 \quad \text{Therefore,} \quad P(3) = {}^4C_3 (0.3)^3 (0.7)^1 = 0.756$$

6) A student takes a 15-question, multiple-choice exam with three choices for each question and guesses on each question. Find the probability of guessing exactly 2 out of 15 correctly. 6) A

- A) 0.060 B) 0.940 C) 0.333 D) 0.133

$n = 15 \quad x = 2$ Three choices, therefore Prob question is correct = $1/3$ $P(2) = {}^{15}C_2 (1/3)^2 (2/3)^{13} = 0.05995$

7) If a student randomly guesses at 20 multiple-choice questions, find the probability that the student gets exactly four correct. Each question has four possible choices. 7) C

- A) 0.218 B) 0.162 C) 0.190 D) 0.085

$n = 20 \quad x = 4$ Each question four choices, $P(\text{correct}) = 1/4 = 0.25$

$P(4) = {}^{20}C_4 (0.25)^4 (0.75)^{16} = 0.189685$

8) A coin is tossed five times. Find the probability of getting exactly three heads. 8) A

- A) 0.313 B) 0.156 C) 0.125 D) 0.800

$n = 5 \quad x = 3 \quad p = 0.5 \quad P(3) = {}^5C_3 (0.5)^3 (0.5)^2 = 0.3125$

9) Find the mean for the values of n and p when the conditions for the binomial distribution are met. 9) A

$n = 700, p = 0.45$

- A) 315 B) 385 C) 173.25 D) 13.2

$\text{mean} = n \times p = 700 (0.45) = 315$

10) The failure rate for taking the bar exam in Philadelphia is 41%. If 375 people take the bar exam, what is the mean for the number of failures? 10) D

- A) 138.1 B) 221.3 C) 90.7 D) 153.8

$\text{mean} = n \times p = 375 \times 0.41 = 153.75$

11) Find the variance for the values of n and p when the conditions for the binomial distribution are met. 11) A

$n = 900, p = 0.3 \quad q = 1 - p = 1 - 0.3 = 0.7$

- A) 189 B) 270 C) 13.7 D) 630

$\text{Var} = n \times p \times q = 900 (0.3) (0.7) = 189$

12) A coin is tossed 72 times. Find the standard deviation for the number of heads that will be tossed. 12) A

- A) 4.24 B) 18 C) 6.78 D) 36

$\text{sqrt means Square Root of} \quad \text{standard dev} = \text{sqrt}(n \times p \times q) = \text{sqrt}(72 \times 0.5 \times 0.5) = 4.2426\dots$