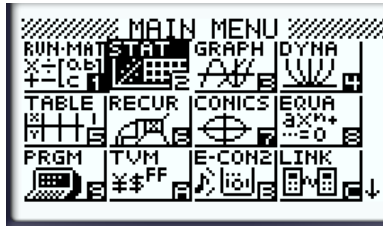
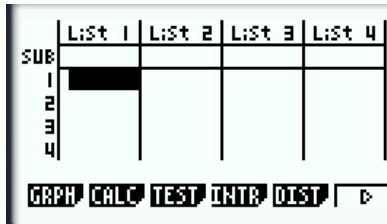


Answers using Casio 9750 GII:

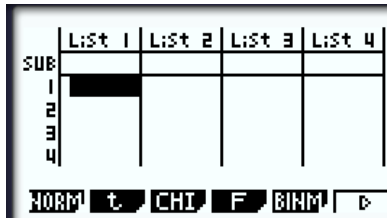
Choose STAT menu:



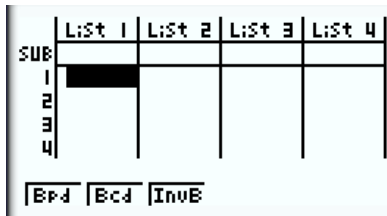
Then, F5 for DIST:



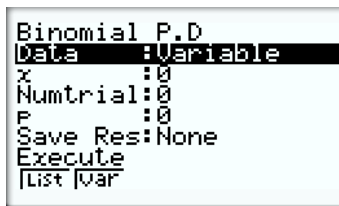
Again F5 for BINM:



Choose F1 for Bpd (This is the same function as binomial pdf):



It looks like this:



Question 1

A multiple-choice test has 10 questions. Each question has four answer choices. What is the probability that a student, choosing answers at random:

1a Gets 7 questions correct (exactly 7)?

Enter $x = 7$, $N = 10$, $p = \frac{1}{4}$

```

Binomial P.D
Data :Variable
x :7
Numtrial:10
P :0.25
Save Res:None
Execute
None LIST

```

Press EXE:

```

Binomial P.D
P=3.0899E-03

```

Scientific notation: 3.0899×10^{-3} Equivalent to 0.0030899

1b. Has at least one question correct?

At last one correct = $1 - P$ no correct (zero correct)

Repeat steps for 1a with $x = 0$, $N = 10$, $p = 1/4$.

```

Binomial P.D
P=0.05631351

```

Then press MENU, and choose RUN-MAT:

Proceed on the main screen to substitute the values into the formula:

At last one correct = $1 - P$ no correct (zero correct) = $1 - 0.0563 = 0.9437$

1c. Has at least 3 questions correct?

P at least 3 questions correct = $1 - [P(0) + P(1) + P(2)]$

In this case we use binomial cdf, which is the “cumulative” value from zero up to a given X , in this case 2.

	List 1	List 2	List 3	List 4
SUB				
1				
2				
3				
4				

For Binomial CDF, choose Bcd; then for $x = 2$, $N = 10$, $p = 1/4$.

```

Binomial C.D
Data :Variable
x :2
Numtrial:10
P :0.25
Save Res:None
Execute
|CALC

```

```

Binomial C.D
P=0.5255928

```

P at least 3 questions correct = $1 - 0.5255928 = 0.4744$ rounded to 4 decimal places.

1d. Has at most 1 question correct?

“At most” means from zero to a number x , in this case 1. Therefore, we use binomial Cdf:

```
Binomial C.D
Data      :Variable
x         :1
Numtrial:10
P        :0.25
Save Res:None
Execute
|CALC
```

Execute:

```
Binomial C.D
P=0.24402523
```

1e. Has at most 4 questions correct?

Binomial cdf, set $x = 4$:

```
Binomial C.D
Data      :Variable
x         :4
Numtrial:10
P        :0.25
Save Res:None
Execute
|CALC
```

Execute:

```
Binomial C.D
P=0.92187309
```

1f. Has all questions correct?

For all questions correct, set $x = 10$. That is 10 out of 10 correct, binomial pdf:

```
Binomial P.D
Data      :Variable
x         :10
Numtrial:10
P        :0.25
Save Res:None
Execute
|CALC
```

Execute:

```
Binomial P.D
P=9.5367E-07
```

Scientific notation: 9.5367×10^{-7} or 0.00000095367 as a decimal.

1g. Has all questions wrong?

All questions wrong means zero correct. Binomial pdf:

```
Binomial P.D
Data      :Variable
x         :0
Numtrial:10
P        :0.25
Save Res:None
Execute
|CALC
```

Execute:

```
Binomial P.D  
P=0.05631351
```

1h. What is the mean number of correct questions the student may expect?

Means of the binomial distribution

$$\mu = n \cdot p = 10 \cdot \frac{1}{4} = 2.5$$

1i. What is the standard deviation of the variable *number of questions correct*?

$$\sigma = \sqrt{n \cdot p \cdot q} = \sqrt{10 \cdot \frac{1}{4} \cdot \frac{3}{4}} = 1.37$$

Note: $q = 1 - p = 1 - \frac{1}{4} = \frac{3}{4}$.

1j. What is the minimum and maximum usual values of correct questions the student may expect:?

The minimum usual value is given by $\mu - 2\sigma$: $2.50 - 2(1.37) = -0.24$

The interpretation of this result: if someone answer 10 questions at random, with a probability of $\frac{1}{4}$ of being correct on each instance, it will be "usual" getting all questions wrong (zero correct). The value -0.24 doesn't have a physical meaning, since no one can go lower of zero correct.

The maximum usual value is given by $\mu + 2\sigma$: $2.50 + 2(1.37) = 2.5 + 2 \cdot 1.37 = 5.24$ So the test taker may expect up to 5 questions correct. Anything above that result will be "unusual" or exceptionally high.

1k. May we consider 6 as a usual number of correct questions under the conditions of this experiment?

Six questions correct would be an unusual high number of correct answers under the conditions of this experiment.